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Estimating the error in equivalent dose values obtained from SAR

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Abstract
Central to all aspects of application of SAR (Single-Aliquot-Regenerative-dose) procedures to dating is the accurate estimation of errors in equivalent dose values (Dₑ). Some approximation approaches have been outlined by others. Here a more rigorous approach is outlined that incorporates the contributions to the total error in Dₑ from not only error in L₀/T₀ (undosed and unbleached ratio) and the contribution from the scatter of data about the best-fit curve, but also contributions from errors in the best-fit regression parameters and from their covariances. Unequal weighting of data points is included. Algorithms and procedures are detailed for two [saturating exponential (E), and saturating exponential-plus-linear (E+L)] of the 4 most common dose-response models [which include linear (L) and quadratic (Q)]. Computed Dₑ values and errors are compared for 6 new and three previously published data sets, using the approach of this paper and two of the approaches of Duller (2007). Differences in Dₑ and its error estimate from these comparisons are often, but not always, small and insignificant, thus indicating that errors in best-fit parameters and their covariances make a small contribution to total error in Dₑ in most situations. One example data set evaluates the effects of dose-point spacing on the estimated Dₑ error.

Introduction
As in Duller (2007), Berger (1990, hereinafter "B90") and Berger et al. (1987, hereinafter, "BLK87"), and some other authors (e.g., Grün and Rhodes, 1992), the error analyses presented herein are intended to capture the effects of random errors, not systematic errors. Discussions about the relative role of random and systematic errors in the construction of dose-response curves (DRCs) for TL (thermoluminescence), ESR (electron spin resonance), and OSL (optically stimulated luminescence) have been joined by many authors (e.g., BLK87; Grün and Rhodes, 1992; Grün and Packman, 1993; Hayes et al., 1998; Galbraith, 2002). In the case of SAR applications, low signals could lead to dominance of systematic errors whereas larger signals are expected to lead to dominance of random errors in L/T ratios (test-dose-normalized OSL in the SAR approach).

The widely used Analyst software package that accompanies the Risø luminescence reader systems provides SAR Dₑ regression procedures for the L, Q, E and E+L DRC models.

The Dₑ error estimation procedures of Analyst are summarized by Duller (2007). His procedure essentially combines in quadrature two components of the total analytical error in Dₑ: an interpolated-range (L₀/T₀ ±error) effect, and the effect of scatter (Duller's equation 7) of L/T ratios about the best-fit curve. This interpolated-range procedure is adopted here in the E+L regression model. Duller's (2007) approach does not capture the effects of errors in the fitting parameters, nor any effects of covariances among the errors in these parameters. His approach does, however (Duller, pers. comm., 2010) incorporate the effects of assigning unequal weights to the data points, where weighting is by inverse variance of the estimated absolute errors in L/T ratios.

The importance of weighting in regression and error analysis has been emphasized and discussed elsewhere (e.g., BLK87; B90; Grün and Rhodes, 1992; Grün and Packman, 1993; Hayes et al., 1998) with regard to constructing DRCs for extrapolation to Dₑ values (in TL and ESR dating). For such extrapolated regressions, Hayes et al. (1998) point out that Bluszcz (1988) discussed how to deal (using the Monte Carlo approach) with TL/ESR cases of mixed error types (e.g., combinations of constant absolute errors, variable absolute errors, constant relative errors). The above cited authors point out (implicitly or explicitly) that dominance by systematic errors implies constant absolute errors, while dominance by random errors can imply constant relative errors. Grün and Rhodes (1992)
conclude that the effects of constant relative errors can be captured by use of weighting by inverse variance, and that this choice leads to smaller errors in estimated D_e values from extrapolated saturating-exponential (hereinafter, 'E fit') TL/ESR DRCs than does the use of equal weighting, which captures the effects of constant absolute errors. This conclusion of Grün and Rhodes (1992) supports the choice of BLK87 for the use of weighting by inverse variance in the calculation of D_e errors from extrapolated DRCs.

While the above efforts concerned extrapolation of DRCs, SAR employs interpolation (as does the regeneration TL procedure). Therefore, estimation of errors in SAR D_e values may have a different dependency on the germane empirical factors than in the case of extrapolations. With SAR, because of the nature of the measurement of L/T ratios, estimation of variance in each SAR dose-data point is quite tractable (e.g., Galbraith, 2002). Thus use of weighting by inverse variance of L/T ratios as presented in this paper is straightforward, avoiding the kinds of uncertainties embedded with the measurement of (for example) TL signals (e.g., BLK87, Appendix A).

Here the mathematical procedures of BLK87 and B90 are adapted to the SAR conditions. BLK87 and B90 used the Gauss-Newton method of linearization of the mathematically non-linear E and E+L models to obtain fitting parameters, and the 'delta' method to obtain error estimates in the extrapolated D_e values. The procedures of BLK87 are statistically accurate when relative errors in the data points are small (e.g., <5%).

Results from these adapted procedures are compared below to the results from the two error-estimation approaches of Duller (2007) as executed in Analyst 2007 (v.3.24): his 'curve-fitting' and Monte Carlo approaches. His 'curve-fitting' approach captures the effects mentioned above (error in L0/T0, unequal weighting, data scatter about the DRC). His Monte Carlo approach presumably captures the end effects of all empirical variables. As Duller (2007) reminds us, when L0/T0 is near the saturation value of E fits, the error in D_e, likely will not be symmetrical. In this situation, only the Monte Carlo approach may yield a statistically accurate estimate of the error in D_e. To construct the best-fit DRCs, Duller (2007) employed the Levenberg-Marquardt (L-M) algorithm. This has many advantages (e.g., Press et al., 1986; Hayes et al., 1998), not the least of which can be speed of convergence for mathematically non-linear models. Essentially then, the algorithms of this paper employ weighting of L/T ratios by inverse variance of same, and, moving beyond the approach of Duller (2007), capture the effects of errors and covariances in fitting parameters.

Although the models presented below force the dose-response curve through the origin, they could be modified to permit passing the regression through the recuperation datum. The 'curve-fitting' procedure of Duller (2007) passes the regression curve through the recuperation datum, but his Analyst software permits the choice of forcing the curve through the origin. Since one of the data-acceptance criteria (e.g., Wintle and Murray, 2006) in the use of SAR is the rejection of data for which the recuperation is >1σ or >2σ from zero, forcing the curve through the origin is likely to be usefully accurate in almost all SAR situations. Furthermore, it has been demonstrated empirically (e.g., Ballarini et al., 2007; Berger, 2009; Berger et al., 2010; Cunningham and Wallinga, 2010) that placing the interval selected for 'background' subtraction close to the beginning part of the OSL decay curve, rather than at the end, often has the effect of reducing the recuperation signal to near zero.

Some Nomenclature

The following terms are employed: \( \sigma^2 \) = absolute-error variance; N = number of L/T (hereinafter, "y") data points, including the origin; w = weight, which for SAR is \( \frac{1}{\sigma_y^2} \); \( y_0 = L_0/T_0 \); \( \theta = a \) fitting parameter (e.g., a, b, or c below); scalar \( \text{VAR} = \text{weighted sum of squares of residuals} \) (an estimate of the scatter of data about the best-fit curve). Note that \( \sigma_y^2 \) can be calculated appropriately by the method of Galbraith (2002). Symmetrical matrix SIG is the matrix \( \Psi \) of equation 10 in BLK87 and of equation 4 in B90; and

\[
\text{SIG} = \text{VAR} \cdot (I)^{-1} \quad (1)
\]

That is, SIG is the product of scalar VAR and the inverse matrix of I. Matrix I is the information matrix of BLK87, and thus SIG is the variance-covariance matrix, or error matrix. The diagonal elements of SIG give the variances in the individual fitting parameters, while the off-diagonal elements give the covariances.

Employed throughout this paper is the standard propagation-of-variance equation

\[
\sigma_f^2 = \sum_k \frac{\partial f}{\partial \theta_k} \cdot \left( \sum_i \frac{\partial f}{\partial \theta_i} \sigma_{\theta_i} \sigma_{\theta_i} \right) \quad (2)
\]

where f is the model function for the curve, and the paired terms provide the variances when \( k = s \) and the covariances when \( k \neq s \). The covariance terms can be
ignored (set to zero) only if the errors in the fitting parameters are independently distributed (independent of each other) and symmetrical with respect to positive and negative values. We assume here that these errors are Gaussian (although this assumption is not required in the approach of BLK87), hence symmetrical, but we cannot assume independence of errors in fitting parameters. However, it is assumed realistically that the error in \( y_0 \) is independent of the errors in the fitting parameters. Note that hereinafter, the subscript "i" will be used for summations over the non-zero dose-axis (x) data points.

The elements of the matrix I (when needed below) are derived from equation 11 of BLK87, which reduces to

\[
I_{k,s} = \sum_i \frac{1}{f_i^2} \frac{\partial (f_i)}{\partial \theta_k} \frac{\partial (f_i)}{\partial \theta_s}
\]  

(3)

**Linear Fit**

This model, a linear dose response curve passing through the origin, applies to many young sediments or heated materials. Realistically we assume that there are errors in \( y \), not in \( x \). Using the weighted least-squares principle, we wish to minimize

\[
S = \sum_i w_i (y_i - f_i)^2
\]  

(4)

where \( f = bx \). Deming’s (1964) equation 39 (p. 33) provides a straightforward form of \( S \) that circumvents the need to know \( b \) beforehand, and his equation 34 (p.31) permits easy calculation of slope \( b \).

Inclusion of the effects of scatter of data about the best-fit curve is required. Deming’s (1964) equation 41 (p.34) provides a simple formulation of \( S \) that circumvents the need to know \( b \) beforehand, and his equation 34 (p.31) permits easy calculation of slope \( b \).

The total variance in \( D_E \) is

\[
\sigma_{D_E}^2 = D_E^2 \left[ \frac{(\sigma_y^2)}{b^2} + \left( \frac{\sigma_{y_0}}{y_0} \right)^2 \right]
\]  

(5)

Here we assume realistically that there is no covariance of \( y_0 \) and \( b \), that is, that the errors in \( y_0 \) and \( b \) are independent.

**Quadratic Fit**

This model applies to young sediments for which the dose response curve is supralinear (e.g., Berger, 1987) or to dose response curves that are slightly sublinear. As BLK87 show, in the low dose region of a dose response, a second-order polynomial can be a good approximation to the physically realistic saturating exponential. The Q model is

\[
f = bx + cx^2
\]  

(6)

and we wish to minimize equation 4 to obtain estimates of \( b \) and \( c \).

We use the matrix normal equations, simplified to the case of only one curve (not the intersection of two curves as in BLK87). Then in the case of unequal weights, the coefficients \( b \) and \( c \) are calculated from equation 2 of BLK87. Following the procedural steps of BLK87, we iterate the calculation of \( b \) and \( c \) until the difference between successive estimates meets some pre-set convergence limit. The \( D_E \) value is the absolute value of the solution to equation 6 when \( f \) is replaced by \( y_0 \) and \( x \) is replaced by \( D_E \).

To obtain the errors in \( b \) and \( c \), we need scalar \( \text{VAR} \) and matrix I from equation 1. Then

\[
\text{VAR} = \frac{\sum_i w_i (y_i - f_i)^2}{N-3}
\]  

(7)

with denominator \( N-3 \) because there are only two fitting parameters. From equation 3, the elements of matrix I are \( I_{bb} = \sum_i w_i x_i^2 \quad I_{cc} = \sum_i w_i x_i^4 \quad I_{bc} = I_{cb} = \sum_i w_i x_i^3 \). Here, the covariances (off-diagonal elements) are not zero because the errors in \( b \) and \( c \) are not independently distributed. Therefore, using equations 1 and 7, we obtain the elements \( \text{SIG}_{bb}, \text{SIG}_{cc}, \text{SIG}_{bc} \) of the error matrix SIG.

The total variance in \( D_E \) follows from equation 2 as

\[
\sigma_{D_E}^2 = \left( \frac{\sigma_f}{\sigma_y} \right)^2 \sigma_y^2 + 2 \left( \frac{\sigma_f}{\sigma_b} \right) \sigma_b^2 \sigma_y^2 + \left( \frac{\sigma_f}{\sigma_c} \right)^2 \sigma_c^2 \sigma_y^2 + 2 \sigma_b \sigma_c \sigma_f \sigma_y \quad \text{SIG}_{bb} + \text{SIG}_{cc} + \text{SIG}_{bc}
\]  

(8)

where we assume reasonably that the error in \( y_0 \) is independent of the errors in \( b \) and \( c \). Therefore, applying equation 8 to the analytic formula for \( D_E \) (solution to equation 6), equation 8 becomes

\[
\sigma_{D_E}^2 = \left( \frac{\sigma_y}{Z} \right)^2 + \left( \frac{b}{2c(Z-1)} \right)^2 \text{SIG}_{bb} + \left( \frac{y_0-ZD_E}{Z} \right)^2 \text{SIG}_{cc} + 2 \left( \frac{b}{2c(Z-1)} \right) \left( \frac{y_0-ZD_E}{Z} \right) \text{SIG}_{bc}
\]  

(9)

where \( Z = |b^2-4c(-y_0)| \).
Saturating Exponential (E)

This model has the most general applicability to charge-trap physical processes, for which trap-type filling at high doses can occur. The model is

\[ f = a(1 - e^{-bx}) \]  

and we wish to minimize equation 4 to obtain estimates of parameters \( a \) and \( b \). From equation 10,

\[ D_e = \frac{1}{b} \ln \left[ \frac{a}{a - y_0} \right] \]  

since \( f = y_0 \) when \( x = D_e \).

Regression to obtain \( a \) and \( b \)

We use the matrix methods and follow the steps of BLK87. The suggested procedure of BLK87 begins with obtaining initial (trial) estimates of \( a \) and \( b \) by setting the weight matrix = 1 and using a quadratic form of the dose-response curve. This step gives initial estimates of \( a \) and \( b \).

Then using estimated (calculated) weights, we find increments to \( a \) and \( b \) using equation 9 of BLK87. In practice, equation 9 can be reformulated (BLK87 matrix symbol \( \beta \) replaced here by matrix symbol \( \Delta A \)) to:

\[ \Delta A = ([WU]^T[WU])^{-1}([WU]^T[WW^*]) \]  

where the matrix elements are:

\[ w_{u_a} = (1 - e^{-bx_i})\sqrt{w_i}, \]
\[ w_{u_b} = ax_i e^{-bx_i}\sqrt{w_i}, \]
\[ w_{y^*} = y_i - a(1 - e^{-bx_i})\sqrt{w_i}. \]

Equation 12 is iterated to the desired level of convergence of \( a \) and \( b \). Then \( D_e \) is calculated from equation 11.

Error in \( D_e \)

We use equation 2, with the \( D_e \) from equation 11 replacing \( f \) in equation 2. Thus the variance in \( D_e \) is calculated from equation 8 (with \( b, c \) replaced by \( a, b \) respectively). Using equation 10, we obtain the elements of I:

\[ I_{aa} = \sum_i w_i, \]
\[ I_{bb} = \sum_i w_i (x_i e^{-bx_i})^2, \]
\[ I_{ab} = \sum_i w_i f_i e^{-bx_i}. \]

Elements of SIG are obtained from equation 1. Using equation 11 for \( D_e \), the partial derivatives in equation 8 become:

\[ \frac{\partial D_e}{\partial y_0} = [b(a - y_0)]^{-1}, \]
\[ \frac{\partial D_e}{\partial a} = -y_0/ab(a - y_0) \]
\[ \frac{\partial D_e}{\partial b} = -D_e/b. \]

These results then permit the calculation of the variance in \( D_e \).

Saturating Exponential Plus Linear (E+L)

This model, as stated by B90, is physically realistic when charge-trap creation occurs at high doses. The linear term can represent the trap-type creation region of the dose response curve. Dose response curves with apparent linear growth superimposed upon a saturating exponential growth have been observed under laboratory irradiations in TL dating (e.g., B90) and quartz SAR OSL dating (e.g., Murray et al., 2008; Pawley et al., 2008). Does this E+L laboratory response of test-dose-normalized OSL require the assumption of E+L trap filling under natural irradiation (sediment burial) conditions?

Notwithstanding this question, comparison of quartz SAR OSL age estimates derived from use of an E+L dose response curve model with independent ages have shown good agreement at ~ 200 ka (Seyda River sites, Murray et al., 2008) and at ~ 450 ka (Pawley et al., 2008). On the other hand, Lai (2010) reported dramatic age underestimation for old loess when E+L dose response curves were observed. Could this underestimation be partly an effect of differences in his SAR procedure from those of others (e.g., Murray and Wintle, 2003)?

There is another physically realistic model that can mimic an apparent E+L dose response curve in SAR, and this is the 'double-saturating-exponential' (DSE) model (e.g., Wintle and Murray, 2006). Here the apparent linear term can manifest a second set of charge traps with a different (larger) saturation level than the first type. Murray et al. (2007) employed this model with SAR data for quartz from their Sula River sites, but obtained age underestimates. Murray et al. (2008) discussed this result, and suggested that perhaps the nature of the geological setting at Sula River and of the independent age assignments might have had more influence on this underestimate than any putative instability in the quartz SAR signal from the high-dose region of the dose response curve. However, in this report only the E+L model is considered for error analysis because this model is much more tractable than the DSE model.

The model is

\[ f = a(1 - e^{-bx}) + cx \]  

(13)
A straightforward, efficient and acceptably accurate path to follow is to use equation 13 to obtain a, b, c, VAR and SIG, then to use

\[ f' = y_0 - a(1 - e^{-bx}) - cx \]  

(14)
to solve for \( D_e \), because \( f' = 0 \) when \( x = D_e \). Equation 14 can be solved for \( D_e \) very efficiently by using the Newton-Raphson iterative procedure (e.g., McCalla, 1967).

Regression to obtain a, b, c
As for the E case, we use the quadratic model with weights = 1 to obtain initial estimates of a and b. Then we assign an initial estimate for c of (e.g.) 0.005, based on the likely general increase in L/T as a fraction of applied dose in units of sec. With these initial estimates of a, b and c, we use equation 12 to begin the iterative process to refine these estimates toward some limit of convergence. In this case, the elements of matrices WU and WY* become:

\[
\begin{align*}
w_{ua} &= (1 - e^{-bx_i}) \sqrt{w_i} , \\
w_{ub} &= (ax_i e^{-bx_i}) \sqrt{w_i} , \\
w_{uc} &= c x_i \sqrt{w_i} , \quad \text{and} \\
w_{yk} &= [y_i - a(1 - e^{-bx_i}) - cx_i] \sqrt{w_i} .
\end{align*}
\]

Solution for \( D_e \) and error in \( D_e \)
Once we have a, b and c, we can use equations 14 to iteratively solve for \( D_e \). Here, the estimation of errors in \( D_e \) is more complex than for the previous models. An efficient, fast and reasonably accurate procedure is to approximate the total variance in \( D_e \) as

\[
\sigma^2_{D_e}(y_0) = \sigma^2_{D_e}(\theta) + \sigma^2_{D_e}(y_0) \]  

(15)

which is the sum of variances from the effect on \( D_e \) of error in \( y_0 \) and the variance arising from the combination of the effects of data scatter about the best-fit curve with the variances and covariances in the fitting parameters a, b and c.

Error in \( D_e \) arising from error in \( y_0 \)
An historically effective way (and used by Duller, 2007) to estimate the component of variance in \( D_e \) that relates to the effects of the variance in \( y_0 \) is to iterate the solution of equation 14 under 3 conditions:

(i) set \( y_0' = y_0 + \sigma_{y_0} \), obtain \( D_e' \);
(ii) set \( y_0'' = y_0 - \sigma_{y_0} \), obtain \( D_e'' \);
and (iii) set \( y_0^0 = y_0 \), obtain the best-fit \( D_e \).

Although \( \sigma^2_{D_e}(y_0) \) may not always be symmetrical about \( D_e \), it is acceptable to set

\[
\sigma^2_{D_e}(y_0) = [(D_e' - D_e'')/2]^2
\]

(16)

Error in \( D_e \) arising from data scatter and from errors in a, b and c
For this purpose we can use the efficient equation 4 of B90 (with his \( \Psi \) replaced by our SIG), which captures all the effects we wish to incorporate. Then in that equation 4,

\[
\begin{align*}
V' &= \left( \frac{\partial f}{\partial a} \frac{\partial f}{\partial b} \frac{\partial f}{\partial c} \right) \\
\frac{\partial f}{\partial \theta} &= c + ab e^{-bdE} .
\end{align*}
\]

For use in equation 1 we need

\[
\text{VAR} = \sum_i w_i (y_i - f_i)^2 / N - 4
\]

where \( f_i \) is given by equation 13. The elements of I, derived using equation 3, are:

\[
\begin{align*}
I_{aa} &= \sum_i w_i (1 - e^{-bx_i})^2 , \\
I_{bb} &= \sum_i w_i (ax_i e^{-bx_i})^2 , \\
I_{cc} &= \sum_i w_i c x_i^2 , \\
I_{ab} &= I_{ba} = \sum_i w_i a x_i e^{-bx_i} (1 - e^{-bx_i}) , \\
I_{ac} &= I_{ca} = \sum_i w_i a x_i^2 (1 - e^{-bx_i}) , \\
I_{bc} &= I_{cb} = \sum_i w_i a x_i^2 e^{-bx_i} .
\end{align*}
\]

Therefore, with these equations for the elements of matrix I and the equation for VAR, we obtain \( \sigma^2_{D_e}(\theta) \) from equation 4 of B90 and the total variance in \( D_e \) from equation 15 combined with equation 16.

Comparison of Results from Data Sets
Results from 3 error-estimation approaches are compared below. The first two approaches are the ‘curve-fitting’ and Monte Carlo routines of Duller (2007) outlined in the first section and executed in Analyst 2007, and the third is the approach outlined in this paper.

Duller’s data sets
Table 1 lists comparisons of the \( D_e \) and errors for 3 of Duller’s (2007) multi-grain SAR data sets. Duller’s (2007) data set D-4 illustrates a linear (L) regression, and the other two, a saturating exponential (E) (samples D-1 and D-2). The E data sets of Duller (2007) are only somewhat sublinear. There is no significant difference in error estimates (within 1σ)
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This paper

D-4
L
0.71 ± 0.11
± 0.13(Sym)
0.73 ± 0.11

D-1
E
0.70 ± 0.06
± 0.06(Sym)
0.698 ± 0.058

D-2
E
28.50 ± 0.67
± 0.75(Sym)
28.48 ± 0.68

* 1000 repeats were used. 'Sym' means that the D_e distribution is symmetric. Only the uncertainties are reported because the D_e estimates are those from the curve-fitting scheme.

Table 1: Comparison of equivalent dose values, and 1σ uncertainties, for 3 data sets from Duller (2007).

<table>
<thead>
<tr>
<th>Sample</th>
<th>FUS-1 (1-70)</th>
<th>FUS-1 (2-20)</th>
<th>FUS-1 (4-40)</th>
<th>SFC-6 (A-10)</th>
<th>SFC-6 (A-15)</th>
<th>ATP-37 (A-1)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Dose (s)</td>
<td>L/T</td>
<td>L/T</td>
<td>L/T</td>
<td>L/T</td>
<td>L/T</td>
<td>L/T</td>
</tr>
<tr>
<td>Natural</td>
<td>1.390 ± 0.378</td>
<td>1.261 ± 0.383</td>
<td>1.703 ± 0.538</td>
<td>Natural</td>
<td>4.957 ± 0.208</td>
<td>2.671 ± 0.212</td>
</tr>
<tr>
<td>100</td>
<td>0.091 ± 0.110</td>
<td>0.324 ± 0.139</td>
<td>0.200 ± 0.234</td>
<td>100</td>
<td>1.109 ± 0.053</td>
<td>1.146 ± 0.107</td>
</tr>
<tr>
<td>300</td>
<td>0.352 ± 0.127</td>
<td>0.900 ± 0.455</td>
<td>0.750 ± 0.322</td>
<td>250</td>
<td>2.129 ± 0.092</td>
<td>2.023 ± 0.195</td>
</tr>
<tr>
<td>1000</td>
<td>1.452 ± 0.483</td>
<td>1.909 ± 0.796</td>
<td>1.783 ± 0.649</td>
<td>500</td>
<td>3.278 ± 0.137</td>
<td>2.165 ± 0.178</td>
</tr>
<tr>
<td>0</td>
<td>-0.036 ± 0.037</td>
<td>-0.074 ± 0.057</td>
<td>0.001 ± 0.001</td>
<td>1000</td>
<td>4.306 ± 0.172</td>
<td>3.420 ± 0.288</td>
</tr>
<tr>
<td>Recycle</td>
<td>1.0 ± 1.6</td>
<td>1.01 ± 0.58</td>
<td>2.4 ± 3.0</td>
<td>2000</td>
<td>5.592 ± 0.226</td>
<td>3.390 ± 0.269</td>
</tr>
<tr>
<td>0</td>
<td>-0.023 ± 0.012</td>
<td>-0.022 ± 0.024</td>
<td>2800</td>
<td>4.558 ± 0.108</td>
<td></td>
<td></td>
</tr>
<tr>
<td>Recycle</td>
<td>0.87 ± 0.06</td>
<td>1.07 ± 0.14</td>
<td>3600</td>
<td>4.853 ± 0.114</td>
<td></td>
<td></td>
</tr>
<tr>
<td>4200</td>
<td>5.091 ± 0.120</td>
<td></td>
<td></td>
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<tr>
<td>5000</td>
<td>5.441 ± 0.128</td>
<td></td>
<td></td>
<td></td>
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</tr>
<tr>
<td>5800</td>
<td>5.737 ± 0.135</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
<tr>
<td>7000</td>
<td>6.102 ± 0.143</td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>0</td>
<td>0.005 ± 0.002</td>
<td></td>
<td></td>
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<td></td>
</tr>
<tr>
<td>Recycle</td>
<td>0.88 ± 0.03</td>
<td></td>
<td></td>
<td></td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

* In parenthesis, either the 'single'-grain hole (e.g., disc 1, hole 70) or the multi-grain aliquot number. The recycle ratio is for the first applied dose. The FUS and SFC samples are quartz sand grains (respectively, 125-185 µm and 105-212 µm). The ATP-37 sample is 4-11 µm quartz.

Note: Most L/T errors in this table are listed with a precision of 3 significant digits even though it is well known that most data error estimates themselves have uncertainties typically of 10-30% (e.g., Topping, 1962, p. 89-90). The retention of 3 significant digits is intended to minimize any effects of round-off error for those users who wish to employ these data in comparisons of results from their own models with the models in this paper. These L/T ratios are from the screen display of Analyst, which truncates errors to the third decimal place. Note also that the absolute errors in the ATP-37 L/T ratios yield approximately constant relative errors (~2.5%).

Table 2: Example data for regression models
among the 3 approaches for the samples D-4, D-1, and D-2. For these data, the fitting parameters (not shown) generated by Analyst 2007 and by the author’s routines do not differ by more than a small fraction of the 1σ uncertainties in these parameters. That is, the respective best-fit DRCs do not differ noticeably.

**Author’s data sets**

The 6 data sets of the author listed in Table 2 illustrate the use of the Q, E and E+L models. Unlike in Duller’s (2007) examples, the dose points in Table 2 are in seconds, not Gy. Other distinctions are in the footnotes to Table 2. The data for the first 3 examples represent SAR conditions for which the relative errors in the L/T ratios are much larger than those in the data sets of Duller (2007). These larger errors manifest the effects of low signals, and so it is likely that the role of systematic errors is larger than would otherwise be the case. Furthermore, these 3 data sets were selected because the scatter of the data about the best-fit DRCs is very small while the absolute and relative errors in the L/T ratios are very large. Finally, the corresponding fitting parameters have very large relative errors (as estimated by Analyst 2007).

The data (excluding recycle and recuperation points) for the 3 different grains of the FUS-1 sample are plotted in Fig. 1, with best-fit regressions of the Q (top), E (middle), and Q (bottom) models. The best-fit DRCs of Analyst 2007 and of the author do not differ on the scale of these plots. All data have large relative errors. The relative errors in the L0/T0 ratios are comparable in all 3 plots. The relative errors in the dose response curve data in the top and bottom plots are comparable, but differ from those in the middle plot. Examples of single-grain data having similarly large relative errors but with more variability within the dose response curve could

**Figure 1:** Top to bottom, Q, E and Q regressions using the routines of this paper for the 'single-grain’ FUS-1 data in Table 2. The percent relative error in each L/T ratio is shown.

**Figure 2:** Comparison of E and E+L best-fit DRCs for sample ATP-37.
probably be found by the author and by readers, but these examples are sufficient to illustrate some differences in the results from the different error-analyses schemes. The $D_e$ and error results from FUS-1 are discussed below after presenting plots for the remaining data in Table 2.

The multi-grain SAR data for the fine-silt (4-11 µm) quartz of sample ATP-37 are presented not only because they provide DRCs having a nearly 'linear' portion beyond a saturating exponential, but also to illustrate the effects on estimated errors in $D_e$ values of variations in the spacing of dose points. The $D_e$ and error results from FUS-1 are discussed below after presenting plots for the remaining data in Table 2.

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It is immediately clear in the top of Fig. 2 that the choice of regression model has a dramatic effect on the value of the estimated $D_e$ and that the weighted E model is inappropriate. An equal-weighting (unweighted) E model has not been applied to these data, but it is not expected to provide an acceptable fit. In the lower Fig. 2, a $D_e$ value could not be computed by either Analyst 2007’s or the author's weighted E-fit routines, because the E fit saturates near the $L_0/T_0$ value. So in this example incomplete knowledge of the DRC could lead to rejection of the aliquot if only an E model were applied.

Figure 3: Comparison of E and E+L best-fit DRCs for sample SFC-6.

data, the dose-doubling scenario can be approximated by eliminating certain dose points in the regressions.

The ATP-37 data for the complete dose range are plotted in the top of Fig. 2, with both E and E+L regressions illustrated. As for the FUS-1 data, the best-fit response curves of the author and of Analyst 2007 are indistinguishable at the plotting scale (the fitting parameters agree within their first 3 digits). The bottom of Fig. 2 shows regressions for an approximate 'dose-doubling' scenario, over a truncated dose range (to 4.2 ks, rather than 7 ks).

It is immediately clear in the top of Fig. 2 that the choice of regression model has a dramatic effect on the value of the estimated $D_e$ and that the weighted E model is inappropriate. An equal-weighting (unweighted) E model has not been applied to these data, but it is not expected to provide an acceptable fit. In the lower Fig. 2, a $D_e$ value could not be computed by either Analyst 2007’s or the author's weighted E-fit routines, because the E fit saturates near the $L_0/T_0$ value. So in this example incomplete knowledge of the DRC could lead to rejection of the aliquot if only an E model were applied.

The final example data set in Table 2 (sample SFC-6) is a dose-doubling set from a multi-grain dating experiment of the author. The best-fit dose response curves are plotted in Fig. 3. Aliquot 10 (top) represents the form of the dose response for most of the 21 aliquots of this sample: apparently an E+L fit is most appropriate. Analyst 2007 provides a 'fit' (estimate of weighted sums of squares of residuals about the best-fit dose response) value of 0.0132 for the E+L model and 0.0959 (~ 7 times larger) for the E model. However, as is shown below, the 3 error-estimation schemes report no statistical difference (at 1σ) in the $D_e$ values from these weighted E and E+L fits.

Aliquot 15 (bottom, Fig. 3) was selected because not only do the data scatter more widely about the best-fit weighted regression dose response, but also the errors in the L/T ratios are much larger than for aliquot 10. In this case, to a first approximation, it could be acceptable to prefer the E+L model based on the assumption that all quartz in this sample should behave the same way. Generally, however, experience shows that quartz dose response curves can vary from grain to grain within a given sample. Therefore, if there are few grains per aliquot, one could expect inter-aliquot differences in dose response.
### Table 3: Comparison of $D_e \pm 1\sigma$ results for the data in Table 2.

<table>
<thead>
<tr>
<th>Sample a</th>
<th>Model b</th>
<th>Curve Fitting</th>
<th>Equivalent Dose (s) Monte Carlo c</th>
<th>This paper</th>
</tr>
</thead>
<tbody>
<tr>
<td>FUS-1/1-70</td>
<td>Q</td>
<td>964±202</td>
<td>±429(Sym)</td>
<td>963±204</td>
</tr>
<tr>
<td>FUS-1/2-20</td>
<td>E</td>
<td>491±219</td>
<td>±295(+Asym)</td>
<td>491±213</td>
</tr>
<tr>
<td>FUS-1/4-40</td>
<td>Q</td>
<td>914±188</td>
<td>±447(-Asym)</td>
<td>914±493</td>
</tr>
<tr>
<td>ATP-37/A-1</td>
<td>E(long)</td>
<td>2104±219</td>
<td>±170(Sym)</td>
<td>2104±128</td>
</tr>
<tr>
<td>E+L(long)</td>
<td>3057±227</td>
<td>±262(Sym)</td>
<td></td>
<td>3056±262</td>
</tr>
<tr>
<td>E+L(short)</td>
<td>sat'n</td>
<td>-</td>
<td></td>
<td>sat'n</td>
</tr>
<tr>
<td>E+L(short)</td>
<td>3095±185</td>
<td>±224(Sym)</td>
<td></td>
<td>3092±251</td>
</tr>
<tr>
<td>SFC-6/A-10</td>
<td>E</td>
<td>1417±769</td>
<td>±171(Sym)</td>
<td>1417±148</td>
</tr>
<tr>
<td>E+L</td>
<td>1489±162</td>
<td>±213(Sym)</td>
<td></td>
<td>1487±172</td>
</tr>
<tr>
<td>SFC-6/A-15</td>
<td>E</td>
<td>502±160</td>
<td>±99(Sym)</td>
<td>--</td>
</tr>
<tr>
<td>E+L</td>
<td>807±299</td>
<td>±314(+Asym)</td>
<td></td>
<td>806±441</td>
</tr>
</tbody>
</table>

Notes:

- 'n-m' indicates 'single-grain' disc-hole number; 'A-n' indicates aliquot number.
- For ATP-37, 'long' means 0-7 ks dose range, while 'short' means 0-4.2 ks.
- 'Sym' indicates a symmetrical distribution in $D_e$ values, whereas '+Asym' denotes asymmetry (high-side skewness) and '-Asym' denotes low-side skewness. For multi-grain aliquots, 700 repeats are used, whereas 1000 repeats are used for single-hole data. *Analyst* 2007 provides a ±1σ error from the Monte Carlo $D_e$ distribution probably by fitting a Gaussian that is centered on the peak of the distribution's histogram. For an asymmetric distribution, this ±1σ error can be misleading. Only error estimates are reported (see footnote 'a', Table 1).
- Although symmetrical, the corresponding Monte Carlo distribution peak occurs at ~1200±~150(1σ) s, not 1417, and moreover, only 58% of the repeats are fitted (~55% when 1000 repeats are selected).
- Does not calculate.
- The Q-fit error estimates for FUS-1(1-70) from Duller's 'curve-fitting' approach and the author's approach are indistinguishable. Although the relative errors in fitting parameters $b$ and $c$ estimated by *Analyst* 2007 are respectively ~50% and ~200%, this agreement between the two approaches implies that the contributions to the total error in $D_e$ from errors in fitting parameters are negligible in this case. However, both $D_e$ errors under-estimate the Monte Carlo error estimate by a factor of about two. Thus for such data (large relative errors, few dose points, little scatter about the best-fit DRC), one should always check the Monte Carlo result before accepting the error estimates from either of the other two approaches.

**The Analyst 2007 'fit' values for 0.118 for the E model, 0.112 for the E+L model are probably effectively the same for aliquot 15. Thus even though it might appear in lower Fig. 3 that the E and E+L models provide distinctly different $D_e$ values, the results in Table 3 below indicate that they do not differ at 1σ. Thus aliquot 15 is a good example of an ambiguous dose response curve that could provide misleading $D_e$ values for a sediment sample containing mixed-age quartz grains. In light of the lessons from the plots in Fig. 2, SFC-6 provides an example of a sample for which a greater number of dose points should have been chosen, not necessarily evenly spaced.**

**Comparison of $D_e$ and errors for the Table 2 data sets**

The $D_e$ and $\sigma_{D_e}^2$ values obtained from the regressions shown in Figs. 1, 2 and 3 are listed in Table 3, along with corresponding values from Duller's (2007) 'curve fitting' and Monte Carlo procedures.
and b are ~100%. Thus the agreement of the D₂ error (±219 s) from the 'curve-fitting' scheme with that (±213 s) from the author's scheme implies that the effect of errors in the fitting parameters on the total D₂ error is negligible in this case also. Nevertheless, a visual inspection of the Monte Carlo D₂ distribution suggests that a more accurate error estimate would be 491±300 s (1σ), and therefore that this 'grain' should be rejected. Caveat emptor!

The error estimates for the Q-fit FUS-1(4-40) also are instructive as to relative performance of the different error-estimation schemes. While the Analyst 2007 Q-fit estimate of ±188 s would imply that this D₂ value should be accepted, the author's scheme produces a much larger estimate (±493 s), suggesting that a closer look at the data is required. Here the estimated relative errors in the fitting parameters b and c are respectively ~50% and ~200%, similar to those for example FUS-1(1-70). Notwithstanding, the author's error estimate is much closer to the Monte Carlo symmetric estimate (±447 s) from Analyst2007, but even this fact is misleading because the Monte Carlo D₂ histogram is highly asymmetric and dramatically skewed to smaller values (negative skewness). A visual inspection of this histogram suggests a more appropriate result of 914±150 s (1σ). Thus in this example, the Duller 'curve-fitting' error-estimation scheme under-performs, and the other two symmetric-error results (Monte Carlo and author's) schemes over-estimate the asymmetric, most-likely error estimates (+150, -350 s).

The ATP-37 data set also offers some useful insights into relative performance of the 3 error-estimation schemes. The full-range ("long") dose E fits give identical D₂ values (2104 s) but apparently different error estimates. From the graph (top Fig. 2) it is apparent that the weighted E fits are not appropriate, and from Table 3 it is clear that the D₂ values from the E+L model are significantly larger than the E-fit values (by ~50%). What is unexpected is the relatively small E-fit error estimate (±128 s) produced by the author's scheme. The Monte Carlo error estimate is near the middle of the range of errors produced by the schemes of the author and of Analyst 2007. These inter-scheme differences for the E model may reflect effects from the use of weighting, but that is a subtlety requiring more study (as suggested by the reviewer, perhaps using numerical simulations, e.g., Grün and Rhodes, 1992). Notwithstanding, the E+L model yields essentially identical results from the 3 approaches, with Analyst2007 giving a 15% (statistically perhaps insignificant) under-estimation of the error (compared to the Monte Carlo result). Is this apparent under-estimation a consequence of not capturing the contributions from the errors and covariances in the fitting parameters? Perhaps only model simulations could answer this question.

Concerning the short-dose regressions, because the L₀/T₀ ratio is at or near the saturation value of the exponential fit, neither Analyst 2007 nor the author's scheme could calculate a D₀ value from the E model. On the other hand, both schemes produced effectively identical D₀ values from the use of the E+L model. Where they differ in this case is that again Analyst 2007's 'curve-fitting' scheme yields the lowest error estimate. Again, this may reflect the neglect of the contributions from the errors and covariances in the fitting parameters. What is also helpful to notice is that any effect of changes in the dose-point spacing (compare top and bottom of Fig. 2) on E+L results when the L₀/T₀ intersection is well within the 'linear' part of the dose response is not statistically resolvable with this data set. This suggests that with SAR, the type of dose-point spacing may not be a significant variable in the estimation of D₀ and its error, as long as the scatter about the best-fit E+L DRC is small.

The final data set (SFC-6) provides an example of dose responses for which a critical variable may be the number of dose points, not the spacing of same. Aliquot 10 of sample SFC-6 apparently yields essentially identical D₀ values whether the E or E+L models are used. However, the error estimates from the use of the E model differ among the 3 schemes, and the Analyst 2007 E-fit Monte Carlo D₀ histogram is anomalous (footnote 'd'). This Monte Carlo routine did not execute to completion (footnote 'd') so the asymmetric D₀ histogram (peak at ~ 1200 s) provides no helpful information about what the statistically realistic D₀ error should be. One could certainly expect an asymmetric Monte Carlo D₀ distribution from this E-fit example, but a symmetric result is generated. The Analyst 2007 'curve-fitting' error estimate of ±769 s for this E fit would appear (from Fig. 3) to be a more reasonable error estimate than those from the other two approaches. For aliquot 10, only the weighted E+L model yields general consistency among the 3 error-analysis schemes, and thus this model is preferred for this aliquot.

As mentioned above, aliquot 15 was selected to represent a dose response having both a larger scatter of L/T ratios about the DRC and larger relative errors (about double) in the L/T ratios than those for aliquot 10. Given the nearness of the L₀/T₀ ratio to the E-fit saturation and the paucity of the dose points, it is surprising how small the error estimates are from the Analyst 2007 'curve-fitting' and Monte Carlo
schemes. Neither seems realistic. On the other hand, all 3 schemes yield E+L model error estimates that overlap at 1σ with the E-fit \( D_e \) estimates.

Notwithstanding, there are differences among the E+L error estimates, with the \textit{Analyst} 2007 'curve-fitting' providing the smallest estimate and the author's scheme, the largest. This largest estimate (±441) appears to reflect more accurately the large spread (at 2σ) of \( D_e \) values within the Monte Carlo histogram than does the 'curve-fitting' error estimate of \textit{Analyst} 2007. However, only the Monte Carlo histogram for the E+L results from aliquot 15 appears to produce a realistic estimate in this case. In particular, this histogram suggests a \( D_e \) value of 807 ± 300 s (1σ). Aliquot 15 yields somewhat ambiguous model results, and without obtaining additional dose points, it is acceptable (to a first approximation) to prefer the E+L model because that seems to be applicable to most of the other aliquots (not shown) from this sample. It is clear that the author's error-analysis scheme could lead to the rejection (\( D_e \) error >50%) of this aliquot, whereas the other schemes would not.

Conclusions
Duller's (2007) 'curve-fitting' approach to estimation of errors in SAR \( D_e \) values, executed in \textit{Analyst} 2007 software, does not capture the contributions from errors in the regression parameters nor from any covariances among the errors in these parameters. The author's error-analysis schemes do capture these contributions. However, comparisons of the computed \( D_e \) values and their error estimates from these two schemes applied to selected data sets generally show no statistically significant differences in error estimates except in special cases.

Moreover, the Monte Carlo scheme executed in \textit{Analyst} 2007 can in some cases indicate a \( D_e \) histogram peak at a value significantly different from the 'central \( D_e \) value' reported by \textit{Analyst} 2007.

Generally, however, for SAR data that have relatively small scatter about the best-fit dose-response curves and that have relative errors in L/T ratios smaller than ~5%, there are no significant differences among the 3 discussed schemes for analysis of L, Q, E and E+L models.

Nevertheless, some data sets (some presented here) can generate misleading \( D_e \) and error estimates, and the practitioner of SAR dating should inspect such data sets carefully before accepting \( D_e \) and error estimates, no matter which error-analysis scheme is employed.

Finally, one selected data set (ATP-37, Table 2) provides a good example of quartz SAR E+L dose response, and is used here to demonstrate that there is (in this case) little or no dependence of computed \( D_e \) values and their error estimates on dose-point spacing schemes, whether spaced evenly or by dose-doubling. This contrasts with the dose-point-spacing dependency shown by the simulations of Grün and Rhodes (1992) for non-SAR data (for which extrapolation is used).

Acknowledgements
Constructive review comments on the first two drafts of this manuscript by Dr. Kristina Thomsen are greatly appreciated.

References


**Reviewer**

K. Thomsen
Thesis Abstracts

Author: Ágnes Novothny
Thesis Title: Luminescence dating of Quaternary aeolian sediments from Hungary
Grade: Ph.D.
Date: December 2008
Supervisor: Manfred Frechen, Erzsébet Horváth
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Loess, loess-like sediments and aeolian sand cover great areas of Hungary. The study areas of this thesis are located in the Gödöllő Hills and along the right bank of the Danube in North-Hungary, both areas are covered by young aeolian sediments.

Different luminescence methods and techniques were applied in order to find the most appropriate protocol to date the sediments of these regions. First IRSL multiple aliquot methods were used for feldspar and polymineral fine grain samples at Albertirsa, Söttő and Tura. The results were in agreement with the previous dating results from Hungary during the 1990s, mostly measured with the same protocol. However, significant age underestimation was observed in all cases, possibly due to anomalous fading of the feldspars. In the next step single aliquot regeneration protocols were applied for quartz and feldspar. The uncorrected IRSL SAR results basically yielded the same results like those of the IRSL MAAD protocol. However, more precise results were obtained by the SAR protocol, especially for very young samples. The main advantage of the SAR protocol over the MAAD method for the samples investigated in this thesis, that fading tests and corrections can be achieved. The fading corrected IRSL ages are more reliable and fit better to the stratigraphical expectations. The younger fading corrected ages (up to 50-60 ka) are consistent with the OSL ages of some quartz samples and with the radiocarbon results. The older fading corrected IRSL ages (90-130 ka) are still underestimated, very likely due to the applied correction method, which is suitable and set up for young samples, or due to the early saturation of the IRSL signal hindering the exact dating of these old samples.

Theoretically OSL dating of the quartz yields more precise ages contrary to the feldspar ages, since the quartz does not suffer from anomalous fading. Unfortunately the OSL properties of the quartz were poor in all samples. Some samples yielded results from the Tura section despite of their dim OSL signal. It is likely, that the glacial material from the Alpine region, carried by the palaeo-Danube, is responsible for the poor luminescence properties of the quartz minerals in both investigated regions.

Summarising the results, the dating of the Söttő and Tura profiles using IRSL MAAD and SAR protocols makes connection between the dating carried out in the past and will be carried out in the future. In a stratigraphical point of view the most important result, that the age of the last interglacial soil, can be found at Söttő, seems to be confirmed by chronological methods like amino acid racemization and luminescence.

Author: Qi-Shun Fan
Thesis Title: Quartz optically stimulated luminescence chronology for high lake level periods in the eastern Qaidam Basin, northeastern Qinghai–Tibetan Plateau since late Quaternary and its palaeoenvironmental implications
Grade: PhD
Date: June 2009
Supervisors: Hai-Zhou Ma and Zhong-Ping Lai
Address: Key Laboratory of Salt Lake Resources and Chemistry, Qinghai Institute of Salt Lakes, CAS, XiNing 810008, P.R.China.

Qaidam Basin is located in the northeastern Qinghai–Tibetan Plateau (QTP), which deposited many lakes (salt lakes now) and preserved a series of shorelines or highstand lacustrine sediments around some lakes. Controversy exists regarding the chronology for high lake levels of lakes in the QTP. Significant efforts have been invested to define the timing of palaeoshoreline deposits using radiocarbon dating on the QTP, and ‘pan–lake period’ (40~28 ka BP), ‘the greatest lake period’ (40~25 ka BP) or ‘rather warm and humid period’ (40~30 ka BP) has been proposed in Late Marine Isotope Stage (MIS) 3. Also using 14C dating, similar observations were reported from adjacent regions, such as the Tengger Desert, the Badain Jaran Desert and the Taklamakan Desert in western China. In recent years, however, others argued that Qinghai Lake, located in the east
of Qaidam Basin on the northeastern QTP, developed a large lake in the period of 110–75 ka (corresponding to MIS 5). Lake level is even lower than present during MIS 3.

Therefore, the aim of this study is to establish the quartz OSL chronology, using SAR protocol, for high lake level periods in the eastern Qaidam Basin and discuss evolution history of Gahai Lake, Toson Lake and Shell Bar based on the geomorphic evidence of lakeshore sediments and environmental proxy (carbonate content) of Shell Bar section. It is concluded that:

1. By analyzing laboratory tests (such as preheat plateau, dose recovery test, growth curves and scatter of $D_e$ for samples), the results indicate that the SAR protocol is appropriate for $D_e$ determination for lacustrine deposits in the eastern Qaidam Basin.

2. OSL dating results show that high lake levels of Gahai Lake, Toson Lake and Shell Bar in the eastern Qaidam Basin occurred in MIS 5, MIS 3 and early-middle Holocene. By comparison high lake level records of lakes in study region with other lakes (Qinghai Lake, Namco Lake) on the QTP, we found that they are almost synchronous, and high lake levels are gradually dropped since MIS 5. The possible mechanism for the formation of high lake levels in the eastern Qaidam Basin was strong Asian summer monsoon.

**Author:** Alexander Kunz

**Thesis Title:** Coastal and dune evolution in south east India revealed by optically stimulated luminescence dating: Reconstruction of sediment dynamic, event history, climatic and environmental change for the last 3500 years

**Grade:** PhD

**Date:** October 2010

**Supervisors:** Brigitte Urban (Leuphana University Lüneburg), Manfred Frechen (Leibniz-Institute for Applied Geophysics)

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Sediments in drylands or coastal areas are good archives for palaeoenvironmental studies. They preserve and reflect changes in climate, events like storms or tsunamis and human impact. The application of dating methods allows establishing a geochronological framework which can be used, e.g., to correlate periods of dune and soil formation to past dry and wet climate conditions or to estimate a recurrence interval for events like storms, tsunamis and earthquakes. The investigation of coastal areas is important as coasts are one of the most dynamic landforms and in many parts of the world densely populated. The impact of events like storms and tsunamis or climatic change has severe consequences on the ecosphere, geosphere and anthroposphere. The knowledge about coastal processes and their timing can help in developing plans for coastal protection and risk assessment.

The aim of this study was to establish a reliable chronological framework for the coastal development of the Andaman Islands and south east India. This framework was used to understand the timing of coastal processes and to reconstruct the genesis of sediments and connect them with events which are indicative for environmental and climatic changes. The dating was done using optically stimulated luminescence (OSL) and radiocarbon. Based on the physical properties of the OSL dating method it is an excellent tool to determine the depositional age of sediments.

On the Andaman Islands coastal sediments have been investigated to find evidence for palaeotsunamis and palaeoearthquakes and to reconstruct the recurrence interval for strong events like the Indian Ocean tsunami from December 2004. Sediment material from event-layers was dated using OSL and radiocarbon dating. The results show evidence for strong earthquakes at around 1000 and 3000 years before present and they reflect the storm activity for the last 1000 years. Also the complex pattern of co- and postseismic uplift and subsidence of the Andaman Islands could be reconstructed.

At the south east coast of India dunes in the Cuddalore area have been investigated. These dunes form a belt running parallel to the coast. A transect from the coast to the most western dune inland was investigated. The dunes show sedimentological features like unconformities, changes in the direction of bedding, erosional features, water escape structures and remnants of human settlement and soil-like horizons which are indicative for environmental changes. The results from the dunes show a connection between the monsoon activity for the last 3500 years and periods of sand movement and stabilisation of dunes. The younger dunes show a connection between periods of reduced rainfall and sand mobilisation for the last 200 years. The investigation of the younger dunes shows also that the dune system in the study area reacts very sensitive to changes in rainfall and disturbances in the landscape.

Based on the dating and sedimentological results of this thesis it can be concluded that the coastal areas...
are very dynamic with rapidly occurring environmental changes. This research draws a clearer picture of the dynamics of coastal environments in south east India and the Andaman Islands and thus provides useful information for coastal zone management planning.

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Grade: PhD
Date: May 2010
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Tidal basins and bar-built estuaries make up 13% of the world’s coastlines. These areas act as important ecosystems for birds and wildlife. Low-lying sand flats within the inter-tidal zone and salt-marshes fringing these tidal basins may be severely threatened by anticipated global warming scenarios, which lead to a sea-level rise. This depends, however, to a large extent on how the sedimentation in these low-lying wetlands responds to an accelerated rate of sea-level rise.

The main objective of this study is to describe the spatial and temporal variability of sedimentation inside tidal basins in order to determine the role of sea-level variations on sedimentation in inter-tidal environments. More specifically, this study investigates whether variations in relative sea-level are the ‘key driver’ for sedimentation by attempting to compare inter-tidal sedimentation rates from three sites that have experienced different sea-level histories.

Sedimentation rates are determined by dating different layers in the sedimentary deposits. Absolute chronologies, obtained using luminescence dating are established from sediment cores, which were recovered in the Danish part of the Wadden Sea (Lister Dyb tidal basin) and in two estuaries in New Zealand (Whanganui Inlet and Parengarenga harbour). The luminescence dating technique assesses the period of time elapsed since quartz and/or feldspar grains were last exposed to daylight, for example as a result of sediment transport in the coastal environment. Radiocarbon dating of underlying peat deposits is used as independent age control to validate the luminescence chronology. The geomorphological and sedimentological evolution during the past few millennia is then described based on investigations of these sediment cores and associated chronologies.

Bioturbation by lugworms lead to post-depositional mixing of the surface sediments that may hamper the establishment of an absolute geochronology. The effects of bioturbation processes on the luminescence ages are therefore investigated. This is done by looking at high-resolution age-depth trends which allows the maximum age offset, the bioturbation rate and a mixing depth of ~20 cm to be determined for a sandy tidal flat in the Wadden Sea. Consequently, the upper ~20 cm of the sediment package (corresponding to 100–200 years of deposition) cannot be used to evaluate temporal trends in sedimentation rates at sandy tidal flats with lugworms, and doing this will lead to serious misinterpretations. However, sedimentary archives from inter-tidal mudflats may be useful to describe the recent (~100 years) temporal trends in sedimentation rates, because preserved sediments are more complete and less disturbed at tidal mudflats than at sandy tidal flats.

High-resolution records of the sedimentation rates of both sandy and muddy tidal deposits have been obtained, despite post-depositional mixing processes. Luminescence dating provides one of the first absolute chronologies for recent to millennial inter-tidal sand deposition in the Wadden Sea, which has been obtained with this degree of detail in time and space. The long-term sedimentation rate averaged over the last few millennia is ~0.7 mm·a⁻¹ in Lister Dyb tidal basin. This is comparable to the relative sea-level rise, which has been observed for the last 2000 years (Szkornik et al., 2008). At a majority of the sites, the sedimentation on the tidal flats is able to keep pace with the relative sea-level rise.

The establishment of sediment budgets for sandy tidal flats is now possible, because the coarse-grained fraction of the sediment in tidal basins can be dated with luminescence dating. This offers new opportunities to the problem of determining contemporary sedimentation of sand. Budgets based on luminescence dating can provide estimates of the total sedimentation in tidal basins in contrast to previous fine-grained sediment budgets that were only based on ²¹⁰Pb dating.

The ratio between variations of relative sea-level and sediment supply controls the sedimentation on the tidal flats and determines whether there is a positive or negative sediment budget inside tidal basins. There is no reason to think that low-lying tidal flats are threatened in the future, as long as the sediment supply continues to be adequate. However, it is questionable whether sediment supply will be sufficient to keep up with an accelerated rate of sea-level rise as projected by all scenarios by the
Intergovernmental Panel on Climate Change (IPCC), and whether the findings from the sediment archive can be extrapolated into the future is still debatable.
Bibliography
Compiled by Daniel Richter

From 1st May 2010 to 31st October 2010


Conference Announcements

13th International Conference on Luminescence and Electron Spin Resonance Dating (LED 2011)

10th-14th July 2011

The conference will take place at the Faculty of Mathematics and Computer Science of the Nicolaus Copernicus University in Toruń, Poland between 10th and 14th July 2011. It is planned for the conference to commence on Sunday morning (10th). The Rectors of both Universities took an honorary patronage over the Conference.

The conference is addressed to researchers developing dating methods relying on trapped charge methods (luminescence and electron spin resonance) and to applying those methods in a wide variety of absolute dating problems. The topics include heated and unheated Quaternary geological, geomorphological and archaeological materials, fundamental studies of basic physical phenomena and related dosimetry as well as advances in instrumentation.

The city of Toruń, founded in 1231, is a treasure of Polish and European history, most importantly, famous for being the home to Nicolaus Copernicus. The city is famous for its remarkable monuments which have won the designation of the cultural heritage of mankind from UNESCO and is visited by a large number of tourists each year.

The conference will be followed up by an optional 4-day (15th to 18th July 2011) post-conference trip to several places of interest in north and south Poland (Medieval castle of Malbork, site of Wapienne and Biskupin, caves near Kraków in the so-called Polish Jurassic Highland, Wieliczka salt mine – UNESCO World Heritage site and the city of Kraków). The trip will conclude in Kraków on 18th July, 2011.

Important deadlines:
28 February 2011: Registration and submission of abstracts
31 March 2011: Early payment

Further information about the meeting can be found at http://led2011.polsl.pl

On behalf of the organizing Committee of LED 2011
UK Luminescence and ESR meeting

12\textsuperscript{th}-14\textsuperscript{th} September 2012

The next UK luminescence and ESR dating research meeting will be held at Aberystwyth University from the 12-14th September 2012. The meeting is intended to provide a forum for the presentation and discussion of the latest research in luminescence and ESR dating and related work. Presentations covering basic physics, methodological issues and the application of these techniques are all welcome. The meeting will consist of both oral and poster presentations, and presentations by research students are particularly encouraged.

Further details will be posted on the Aberystwyth Luminescence Research Laboratory website (http://www.aber.ac.uk/en/iges/research-groups/quaternary/luminescence-research-laboratory) later in 2011.

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Errata: An alternate form of probability-distribution plots for D_e values

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(Received 5 December 2010)

Errata
In the paper by Berger (2010), there are two errors. In the first the author stated that radial plots are not applicable to D_e distributions containing negative D_e values. This is correct only if a logarithmic scale is used (as in the widely circulated radial-plot graphical routine by Olley). The author’s statement is incorrect if a linear scale for D_e values is used (e.g., Fig. 1 in Berger, 2010, from Galbraith, 1988, and of course in Galbraith, 2010, Fig. 5).

The second error is that the author referred to the transformed PD plot as a ‘relative probability’ plot. This is incorrect because a (D_e)^-1 factor [in the partial-derivative transformation of log_e (D_e)] was omitted. The (D_e)^-1 factor was omitted to create a plot yielding roughly constant peak heights for the example data in Fig. 3 of Berger (2010). As such the so-called TPD plot does not manifest relative probabilities (requiring comparison of areas under these peaks), rather something more akin to relative ‘weighted’ frequencies. If the (D_e)^-1 term is retained, then the TPD solid curve in the Fig. 3 of Berger (2010) would look closely alike the original dashed curve in that Fig. 3 (obtained using weighting by absolute errors). Thus the TPD plot (when presented with ranked D_e values) serves as only a visualization of relative (within the range of D_e values) ‘weighted’ frequencies when errors in D_e are mainly constant relative and when the distribution of D_e values is approximately log-normal. Finally, D_e values in the TPD plot were placed on a linear scale because generally we perceive geological time as linear, not logarithmic.

As Berger (2010) and Galbraith (2010) both agree, the appropriate post-visualization steps for calculating usefully accurate and precise age estimates involve the suitable use of either weighted means, minimum-age-models (MAM), central-age-models, etc., coupled sometimes with the display of data in a radial plot.

Acknowledgements
I thank Rex Galbraith for pointing out (pers. comm., 2010) that the omission of the (D_e)^-1 factor precludes inferring relative probabilities from the TPD plot.

References
Submission of articles to Ancient TL

Reviewing System
In order to ensure acceptable standards and minimize delay in publication, a modification of the conventional refereeing system has been devised for Ancient TL:

Articles can be sent directly by authors to a member of the Reviewers Panel chosen on the basis of the subject matter, but who is not in any of the authors’ laboratories. At the discretion of the Editor, reviewers who are not listed in the Panel may be used.

The reviewing system aims to encourage direct dialogue between author and reviewer. The Editor should be kept advised of the progress of articles under review by sending him copies of all correspondence. He is available for advice where reviewing difficulties have arisen. Authors whose mother tongue is not English are required to have their manuscript revised for English before submitting it.

We ask reviewers to specify (where required) the minimum of revision that is consistent with achieving a clear explanation of the subject of the paper, the emphasis being on rapid publication; reviewers are encouraged to make a brief written comment for publication at the end of the paper. Where a contribution is judged not to meet an adequate standard without substantial modification, the author will be advised that the contribution is not suitable for publication. Articles that are not considered to be of sufficient interest may also be rejected.

Procedures
1. Articles should be submitted to an appropriate member of the Reviewing Panel or Editorial Board, chosen on the basis of the subject matter, but who is not in any of the authors’ laboratories.
2. Articles should not normally exceed the equivalent of 5000 words inclusive of diagrams, tables and references. Greater space will be appropriate for certain topics; for these the Editor should first be consulted. Short notes and letters are also acceptable. Text should be double-spaced.
3. Diagrams and labels should be ready for direct reproduction (i.e. 1:1 camera ready) and not normally exceed 12 cm wide by 10 cm high. Where possible, high quality electronic versions of figures should also be submitted. Separate figure captions should be supplied. By ensuring that these requirements are met, authors will be able to examine whether all details of their diagrams are clear to the reader. Inappropriately scaled drawings and labels will be returned for alteration.
4. Authors are asked to submit 1 copy of the paper, including diagrams, to the Reviewer and a duplicate copy to the Editor.

In addition to a hard copy of the accepted version of the paper and original diagrams, the final version of the text must be submitted to the Editor electronically using a standard format (Microsoft Word for PC is currently used for producing Ancient TL). Electronic copies of Diagrams and Tables should also be submitted.
5. Upon receipt of an article, the Editor will send an acknowledgement to the author. If the Reviewer is unable to deal with the contribution within 4 weeks he/she will inform the author and advise the Editor.

Requirements under various situations
When agreement concerning an article has been reached:
The Editor should receive a copy of the final version of the paper, both as hard copy and electronically. The Reviewer should send their final decision, including comments for publication if any, to the Editor.

If the article has not been rejected, but agreement on its final form cannot be reached or where there are protracted delays in the reviewing process:
The Editor may request an assessment from the Reviewer and responsibility passes to the Editor.

If the article is rejected:
The Editor and author receive notification from the Reviewer, with an indication of the reason for rejection.

Thesis abstracts are to be sent to the Editor and in principle do not need reviewing. However, authors are requested to make sure that the English is correct before submission. Thesis abstracts should not exceed 500 words, and figures and tables are not accepted.

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Subscriptions to Ancient TL
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The subscription rate for 201 is £15 for individual subscribers and £25 for Institutional subscription, plus any taxes where required. Payment must be in pounds sterling. Enquiries and orders must be sent to the Editor. Payment may be by cheques, made payable to ‘Aberystwyth University’, by credit/debit cards or by bank transfers. Further information on subscriptions is available on the Ancient TL web site (http://www.aber.ac.uk/ancient-tl)